

# Bridging Symbolic and Sub-Symbolic AI: Towards Cooperative Transfer Learning in Multi-Agent Systems

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Next in Line...

- 1 Motivation & Context
- 2 Symbolic and Sub-Symbolic Tools
- 3 Cooperative (Transfer) Learning
- 4 Conclusions & future works



# Motivation

## The three ways of reasoning

- **induction**: a kind of reasoning that uses particular examples in order to reach a general conclusion about something  
→ machine learning (e.g., neural networks);
- **deduction**: the act or process of using logic or reason to form a conclusion or opinion about something  
→ symbolic artificial intelligence (e.g., logic programs);
- **abduction**: the forming and accepting on probation of a hypothesis to explain surprising facts  
→ abductive logic programming.

## Mimic the human society

- do not be bound for one single type of reasoning;
- **cooperation!** Knowledge sharing and explanation.

[Omicini, 2020]

# Context

## Knowledge representation

- **symbolic** representation → formalism consisting of: [van Gelder, 1990]
  - set of symbols;
  - set of rules enabling possibly infinite combinations of symbols;
  - each (composed) symbol comes with its *meaning*;
  - human readable and **interpretable**;
  - intensional and extensional.
- **sub-symbolic** representation → the knowledge is represented via *numeric* data structures:
  - usually with fixed size;
  - a number does not have a particular meaning *per se*;
  - a number could be meaningful only considering its local context;
  - **obscure**, difficult to interpret.

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# Symbolic Knowledge Extraction

## Symbolic Knowledge Extraction (SKE)

[d'Avila Garcez et al., 2001, Hailesilassie, 2016, Zilke et al., 2016, Guidotti et al., 2018]

*any algorithmic procedure accepting trained sub-symbolic predictors as input and producing symbolic knowledge as output, in such a way that the extracted knowledge reflects the behaviour of the predictor with high fidelity.*

### SKE advantages

- *post-hoc* explanation of sub-symbolic predictors;
- generates a symbolic representation of the predictor's behaviour, usually a logic formalism
  - much more concise w.r.t. the predictor, less space cost;
  - formal logic can be used as *lingua franca* in knowledge sharing.

# Symbolic Knowledge Injection

## Symbolic Knowledge Injection (SKI)

[Besold et al., 2017, Xie et al., 2019, Calegari et al., 2020]

*any algorithmic procedure affecting how sub-symbolic predictors draw their inferences in such a way that predictions are either computed as a function of, or made consistent with, some given symbolic knowledge.*

### SKI advantages

- improve predictor's metrics (e.g., accuracy, f1-score, r2, etc.);
- reduce learning time;
- loosening the need of big datasets;
- prevent the predictor to become a black-box;
- independent from the source of the knowledge.

# Transfer Learning

## Transfer Learning (TL) [Pan and Yang, 2010]

*is the set of techniques aimed at letting a **predictor  $P$** , targetting task  $T$ , take advantage from the **knowledge** acquired by some prior **predictor  $P'$** , trained on some other task  $T'$  (usually similar to  $T$ ).*

## TL properties

- similarly to SKI it improves the predictor's performance
  - inference ability (e.g., accuracy, f1-score, r2, ect.);
  - external metrics (e.g., training time, dataset size, etc.).
- constrained by the (sub-symbolic) knowledge of the first predictor
  - for instance, if we are doing TL from a NN to another, we have to replicate part of it – contiguous layers and weights – to the new one;
  - it is obscure for humans.

# Multi-task Learning

## Multi-task Learning (MTL) [Caruana, 1997, Zhang and Yang, 2022]

*is a set of mechanisms aimed to improve the performance of a predictor via TL. More precisely, given a set of similar tasks  $\{T_1, \dots, T_m\}$ , MTL aims at learning the  $m$  tasks altogether, by training as many **predictors**  $P_1, \dots, P_m$ . In doing so, MTL attempts to improve the performance of each  $P_i$ , by taking advantage of the **knowledge** while training the other predictors.*

## MTL properties

- similarly to TL it improves the predictors' performance;
- unlike TL where there is one task that receives the knowledge from the other(s), all tasks *simultaneously* receive knowledge from the others
  - the simultaneous training has pro and cons;
  - still not interpretable.

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# Cooperative Learning I

## Cooperative Learning (CoL)

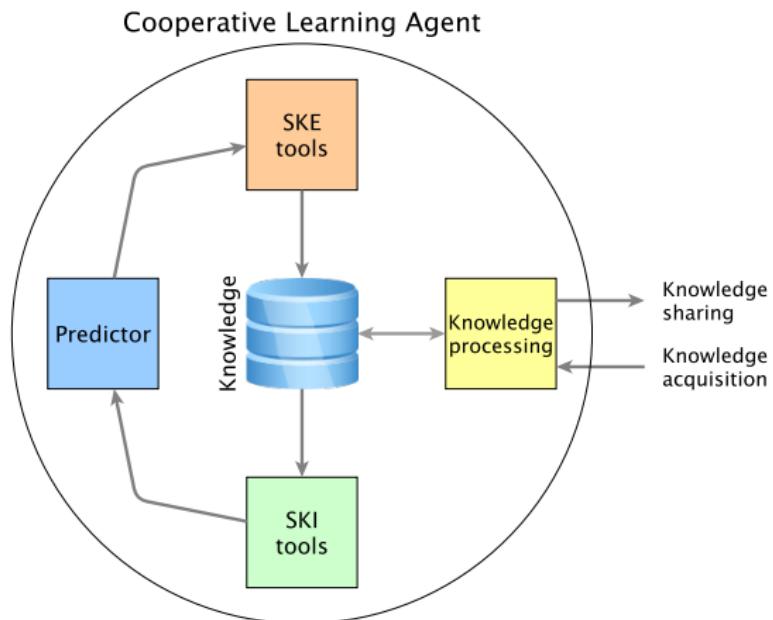
*a CoL system consists of a multi-agent system (MAS) where agents can retrieve and exploit **knowledge** – especially symbolic – about a **task** from other agents and provide it to others when requested.*

## CoL characteristics

- agents should **agree** on common, shared symbolic representation means by which behavioural specifications could be described—and later exchanged;
- agents should come with symbolic (and sub-symbolic) tools for knowledge manipulation.



# Cooperative Learning II



# Cooperative Transfer Learning I

## Cooperative Transfer Learning (CoTL)

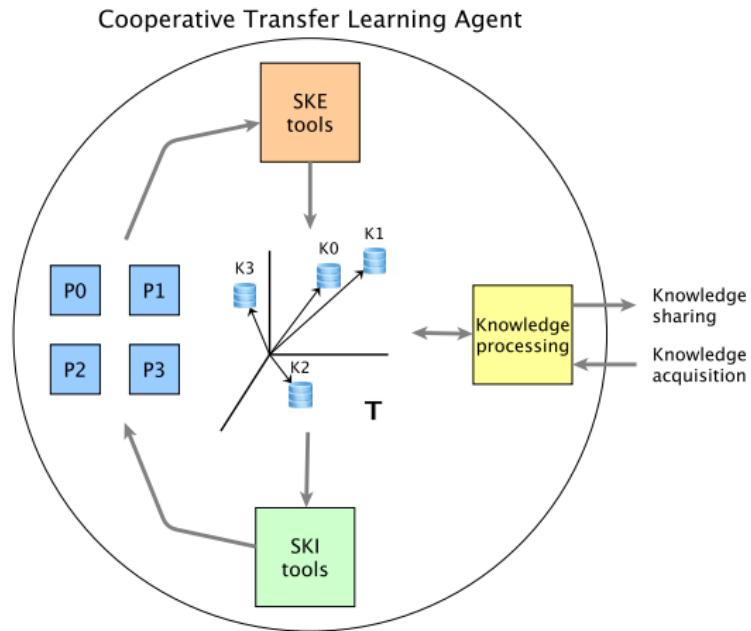
*a CoTL system consists of a multi-agent system (MAS) where agents can retrieve and exploit knowledge about several tasks from other agents and provide it to others when requested.*

### CoTL characteristics

- unlike simple CoL systems, agents in CoTL systems may exploit knowledge (either their own, or other agents' one) about related tasks to learn novel tasks they were not originally designed for  
→ find ways to exploit the knowledge  $K$  of the task  $T$  for a similar – yet not the same – task  $T'$  could be not trivial.



# Cooperative Transfer Learning II



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# Conclusions & (future) works I

## Summing up

Cooperative Learning and Cooperative Transfer Learning are MAS where **cooperation** and **sharing** of (symbolic) knowledge are fundamental inter agents operations. Internally, an agent should be able to manipulate the knowledge in order to exploit it in solving tasks. Key aspects are:

- agreement upon a logic formalism as *lingua franca* for knowledge exchange;
- agents should come with algorithms able to manipulate knowledge (e.g., SKE, SKI, logic engine, etc.);
- how to exploit knowledge in scenarios of *heterogeneous* tasks.



# Conclusions & (future) works II

## Current works

- PSyKE & PSyKI [Sabbatini et al., 2021a, Magnini et al., 2022b]
- SKI algorithms [Magnini et al., 2022a, Magnini et al., 2022c]
- SKE algorithms [Sabbatini et al., 2021b, Sabbatini and Calegari, 2022]

## Future works

- test the *train-extract-fix-inject* workflow;
- create and test CoL systems;
- investigate how to handle knowledge for *heterogeneous* tasks;
- finally, create and test CoTL systems.



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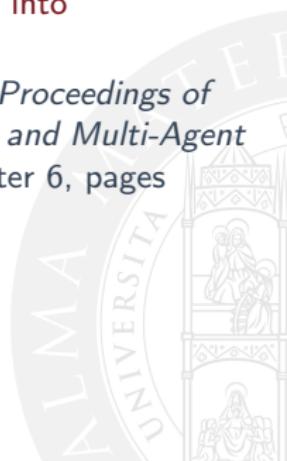
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